

## EQUATION OF STATE OF SODIUM FOR MODELING OF SHOCK-WAVE PROCESSES AT HIGH PRESSURES

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**Summary.** A simple model of equation of state, which represents the relationship of pressure with density and internal energy in the form of an analytic function, is used for sodium in bcc-solid and liquid phases. Thermodynamic characteristics along the principal Hugoniot adiabat are calculated for the metal and compared with available data from shock-wave experiments. The calculation results are in a good agreement with the data over whole investigated region. The equation of state can be used effectively at numerical modeling of shock-wave processes in sodium at high pressures.

### 1 INTRODUCTION

An equation of state (EOS) of a medium is indispensable for numerical modeling of physical processes under intense pulsed influences on materials [1–3]. For example, at high-velocity impact of bodies [4–12], interaction of intense laser [13–24] and particle beams [25–30] with matter, electrical explosion of conductors under action of high power current pulses [31–37] etc. Accuracy of thermodynamic description of properties of the medium over wide range of pressures and densities determine the adequacy of results of the modeling [38].

It is traditional to use semiempirical approach for construction of wide-range EOS models [1, 39–41]. At that, a functional form of a thermodynamic potential is chosen with taking into account theoretical considerations, while numerical coefficients in the function are determined using experimental data.

This work is devoted to description of thermodynamic properties of sodium at high pressures. The metal is used as a coolant in power plants, especially in fast neutron reactors. In particular, EOS for sodium is interesting for numerical modeling of different working regimes of such reactors under conditions of intense mechanical and thermal influences.

In the work, a semiempirical EOS in a form of simple analytic function  $P = P(V, E)$  [42–44] is presented for Na, which is in contrast with more complex EOSs for the metal [45–51]. Here,  $P$  is the pressure,  $V = \rho^{-1}$  is the specific volume,  $\rho$  is the density,  $E$  is the specific internal energy. The quality of proposed EOS is evaluated by a comparison of calculated kinematic and

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dynamic parameters along the principal Hugoniot adiabat with available data from shock-wave experiments.

## 2 EOS MODEL

The EOS model is formulated in the general form as

$$P(V, E) = P_c(V) + \frac{\Gamma(V, E)}{V} [E - E_c(V)], \quad (1)$$

where  $E_c$  and  $P_c = -dE_c/dV$  are the cold components of internal energy and pressure at  $T = 0$ ;  $\Gamma$  is a coefficient determining the contribution of thermal components of the EOS.

The cold energy is given by a polynomial [42–44, 52–54]

$$E_c(V) = \frac{B_{0c}V_{0c}}{m-n} \left( \frac{\sigma_c^m}{m} - \frac{\sigma_c^n}{n} \right) + E_{\text{sub}}. \quad (2)$$

Here,  $\sigma_c = V_{0c}/V$ ;  $V_{0c}$  and  $B_{0c}$  are the specific volume and bulk modulus at  $P = 0$  and  $T = 0$ . The quantity  $E_{\text{sub}}$  has meaning of the sublimation energy and is determined by a condition

$$E_c(V_{0c}) = 0, \quad (3)$$

which gives

$$E_{\text{sub}} = \frac{B_{0c}V_{0c}}{mn}. \quad (4)$$

Parameters  $m$  and  $n$  are determined with the use of shock-wave data for solid samples.

The dependence of the coefficient  $\Gamma$  upon the volume and internal energy is defined analogously to caloric models [42–44, 55–57] in the following form:

$$\Gamma(V, E) = \gamma_i + \frac{\gamma_c(V) - \gamma_i}{1 + \sigma^{-2/3} [E - E_c(V)] / E_a}, \quad (5)$$

where

$$\gamma_c(V) = 2/3 + (\gamma_{0c} - 2/3) \frac{\sigma_n^2 + \ln^2 \sigma_m}{\sigma_n^2 + \ln^2(\sigma/\sigma_m)}, \quad (6)$$

$\sigma = V_0/V$ ;  $V_0$  is the specific volume under normal conditions;  $\gamma_c(V)$  corresponds to the case of low thermal energies, and  $\gamma_i$  characterizes the region of highly-heated matter. The value of  $E_a$ , which defines the thermal energy of the transition of  $\Gamma$  from one limiting case to the other, is determined from the results of shock-wave experiments at high pressures. From (1), (5) and (6), a relation of the parameter  $\gamma_{0c}$  with values of the Grüneisen coefficient  $\gamma = V(\partial P/\partial E)_V$ , the

internal energy and the specific volume under normal conditions ( $\gamma_0$ ,  $E_0$  and  $V_0$ , respectively) can be obtained:

$$\gamma_c = \gamma_i + (\gamma_0 - \gamma_i) \left[ 1 + \frac{E_0 - E_c(V_0)}{E_a} \right]^2. \quad (7)$$

The interpolational function (6) ensures validity of the condition  $\gamma(V_0, E_0) = \gamma_0$ , and gives the asymptotic value  $\gamma_c = 2/3$  in the limiting cases of low and high compression ratios  $\sigma$ . The parameters  $\sigma_n$  and  $\sigma_m$  are determined from the requirement of optimum fit to experimental data on shock compressibility of a substance in question.

### 3 EOS FOR SODIUM

Sodium under atmospheric pressure has a body-centered cubic (bcc) structure ( $T > 6$  K) [58]. It melts at 371 K. Under static compression at room temperature, the bcc phase transforms at pressure 65 GPa to the phase with a face-centered cubic (fcc) structure. At further increase of pressure at room temperature, more crystalline phases of sodium are observed [59–61].

Shock compressibility of sodium is investigated with the use of traditional explosive systems up to 0.1 TPa [62–64]. Shock compression leads to increase of temperature and melting of the bcc phase [49].

In this work, the unified EOS for bcc-solid and liquid phases of sodium is constructed. The EOS coefficients obtained within the framework of the model are as follows:  $V_0 = 1.0331$  cm<sup>3</sup>/g,  $V_{0c} = 0.99306$  cm<sup>3</sup>/g,  $B_{0c} = 6.817$  GPa,  $m = 1$ ,  $n = 0.96$ ,  $\sigma_m = 1.2$ ,  $\sigma_n = 1.5$ ,  $\gamma_{0c} = 0.9$ ,  $\gamma_i = 0.45$  and  $E_a = 45$  kJ/g.

Calculated principal Hugoniot adiabat of sodium is presented in figures 1–3 in comparison with data from experiments [62–64]. Calculation of the Hugoniot adiabat is performed by solving the equation of energy conservation in the shock-wave front [1]:

$$E = E_0 + \frac{1}{2}(P_0 + P)(V_0 - V), \quad (8)$$

where the left-hand side is closed by the EOS function  $E = E(P, V)$ . Equation (8) and the EOS determine the specific volume as a function of pressure along the Hugoniot adiabat for samples of initial density  $\rho_0 = V_0^{-1}$ . Then the shock ( $U_s$ ) and particle ( $U_p$ ) velocities are calculated using the equations of conservation of mass and momentum in the shock-wave front [1]:

$$U_s = V_0 \sqrt{(P - P_0)/(V_0 - V)}, \quad U_p = \sqrt{(P - P_0)(V_0 - V)}. \quad (9)$$

Analysis of the comparison results in figures 1–3 shows that the obtained EOS provides for a reliable description of thermodynamic properties of the metal over a whole investigated range of shock and particle velocities, pressures and compression ratios.

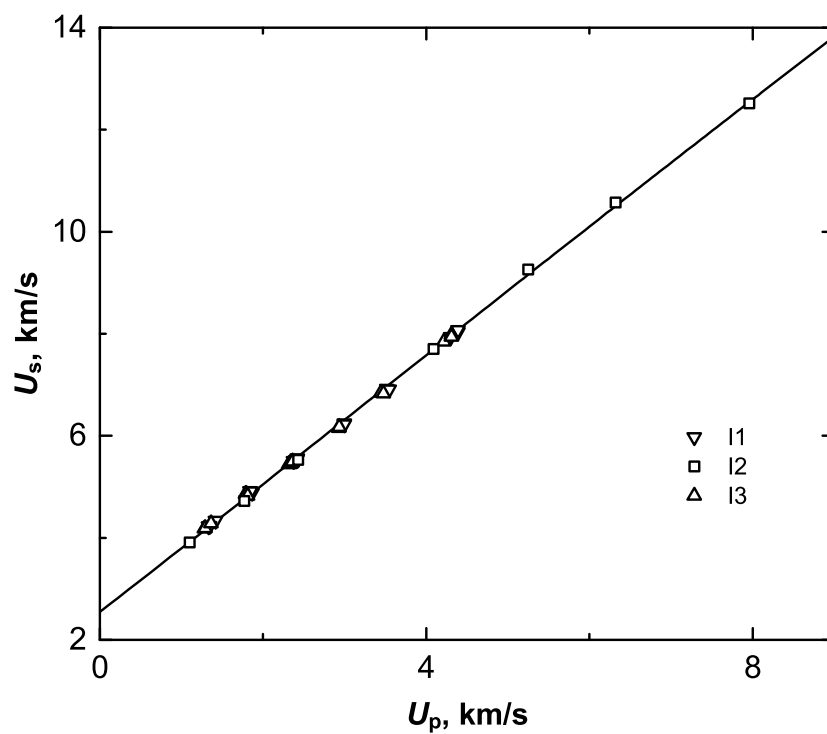


Figure 1: The principal Hugoniot adiabat of sodium: curve corresponds to the present calculations; markers—experimental data (I1—[62], I2—[63], I3—[64]).

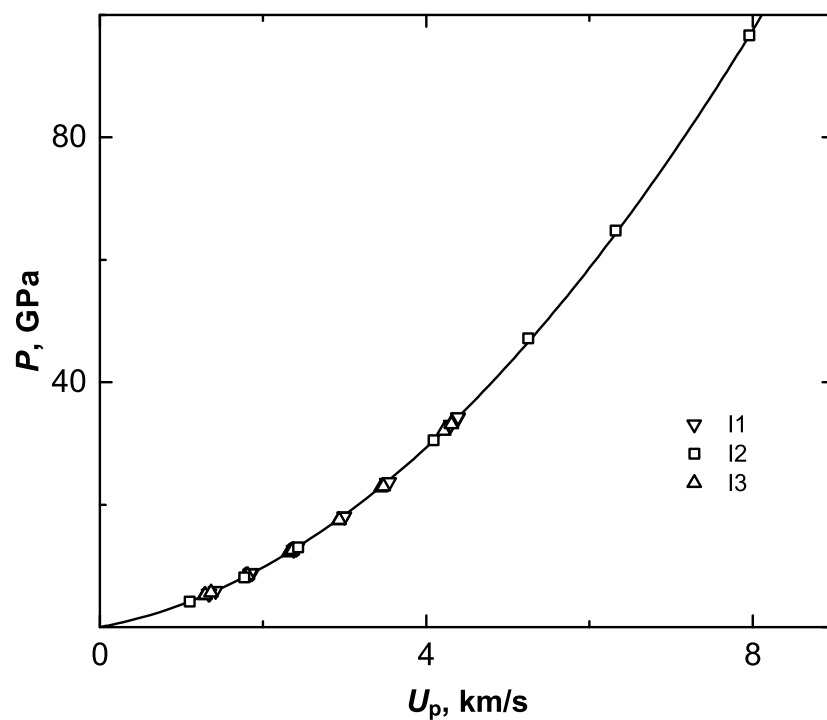


Figure 2: The principal Hugoniot adiabat of sodium: notations are analogous to figure 1.

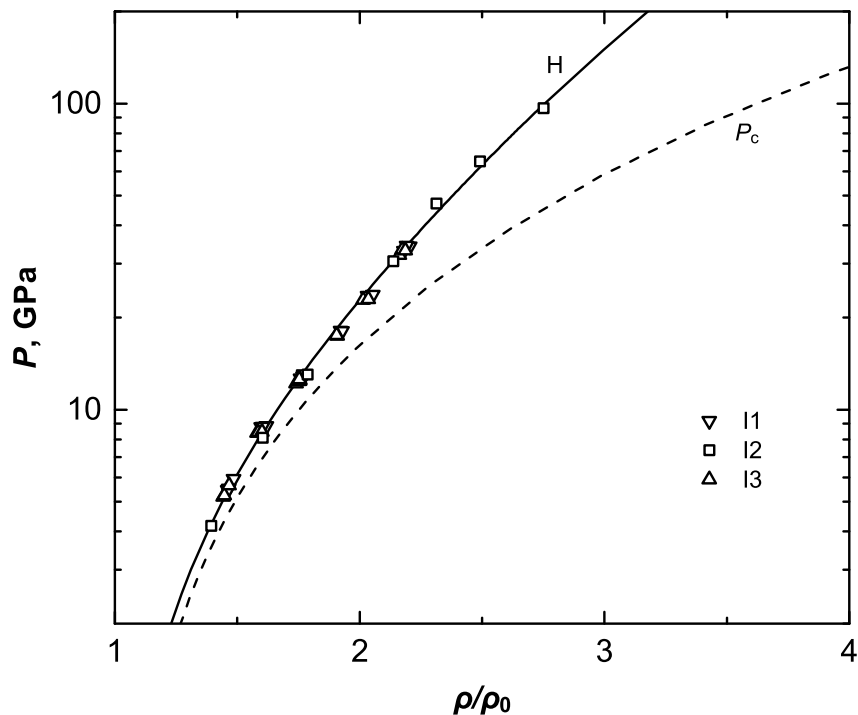


Figure 3: The cold curve ( $P_c$ ) and the principal Hugoniot adiabat (H) of sodium: curves correspond to the present calculations; markers—experimental data (I1—[62], I2—[63], I3—[64]).

#### 4 CONCLUSIONS

The EOS, which has the form of an analytic function, is proposed for sodium in bcc-solid and liquid phases. This EOS agrees well with available data from dynamic experiments; it can be used effectively at numerical modeling of shock-wave processes in the metal at high pressures.

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